

You thought your communication was secure? Quantum computers are coming!

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Cryptography

- ▶ Motivation #1: Communication channels are spying on our data.
- ▶ Motivation #2: Communication channels are modifying our data.



Sender
“Jefferson”



Untrustworthy network
“Eavesdropper”



Receiver
“Madison”

- ▶ Literal meaning of cryptography: “secret writing”.
- ▶ Achieves various security goals by secretly transforming messages.

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www.iacr.org

Your connection to this site is private.

Permissions

Connection

🔒

The identity of this website has been verified by RapidSSL SHA256 CA - G3. No Certificate Transparency information was supplied by the server.
[Certificate information](#)

🔒

Your connection to www.iacr.org is encrypted using a modern cipher suite.

The connection uses TLS 1.2.

The connection is encrypted and authenticated using AES_128_GCM and uses ECDHE_RSA as the key exchange mechanism.

[What do these mean?](#)



2013

iacrmemHEREATiacr.org

1702

Members
(1580 in 2012)

1245

Regular+

457

Students

www.iacr.org

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iacrmemH

170



2013

Secret-key encryption



- ▶ Prerequisite: Jefferson and Madison share a secret key .
- ▶ Prerequisite: Eve doesn't know .
- ▶ Jefferson and Madison exchange any number of messages.
- ▶ Security goal #1: **Confidentiality** despite Eve's espionage.

Secret-key authenticated encryption



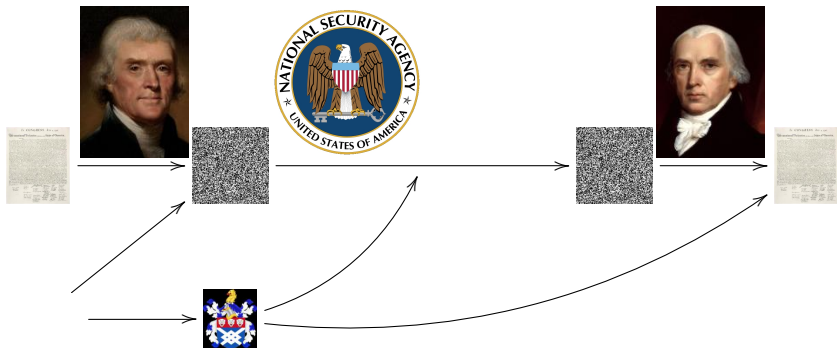
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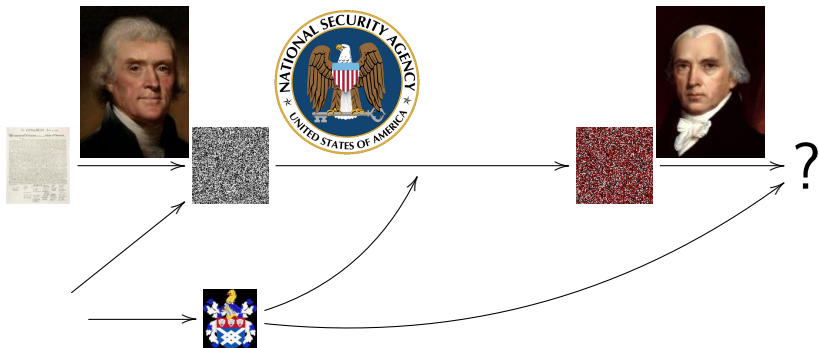
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Public-key signatures



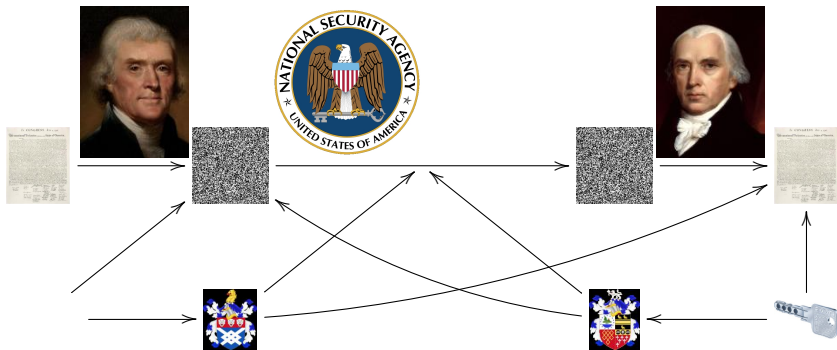
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Public-key authenticated encryption (“DH” data flow)



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- ▶ Jefferson and Madison exchange any number of messages.
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- ▶ Security goal #2: Integrity.

Many more security goals studied in cryptography

- ▶ Protecting against denial of service.
- ▶ Stopping traffic analysis.
- ▶ Securely tallying votes.
- ▶ Searching encrypted data.
- ▶ Much more.

Cryptographic applications in daily life

- ▶ Mobile phones connecting to cell towers.
- ▶ Credit cards, EC-cards, access codes for banks.
- ▶ Electronic passports; soon ID cards.
- ▶ Internet commerce, online tax declarations, webmail.
- ▶ Facebook, Gmail, WhatsApp, iMessage on iPhone.
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Snowden in Reddit AmA

Arguing that you don't care about the right to privacy because you have nothing to hide is no different than saying you don't care about free speech because you have nothing to say.

Cryptographic tools

Many factors influence the security and privacy of data:

- ▶ Secure storage, physical security; access control.
- ▶ Protection against alteration of data
⇒ [public-key signatures, message-authentication codes](#).
- ▶ Protection of sensitive content against reading
⇒ [encryption](#).

Currently used crypto (check the lock icon in your browser) starts with RSA, Diffie-Hellman (DH) in finite fields, or elliptic curve DH, followed by AES or ChaCha20.

Internet currently moving over to [Curve25519](#) (Bernstein) and [Ed25519](#) (Bernstein, Duif, Lange, Schwabe, and Yang).

Security is getting better. Some obstacles: bugs; untrustworthy hardware; anti-security measures such as UK snoopers' charter.



Algorithms for Quantum Computation: Discrete Logarithms and Factoring

Peter W. Shor
AT&T Bell Labs
Room 2D-149
600 Mountain Ave.
Murray Hill, NJ 07974, USA

Abstract

A computer is generally considered to be a universal computational device; i.e., it is believed able to simulate any physical computational device with a cost in computation time of at most a polynomial factor. It is not clear whether this is still true when quantum mechanics is taken into consideration. Several researchers, starting with David Deutsch, have developed models for quantum mechanical computers and have investigated their computational properties. This paper gives Las Vegas algorithms for finding discrete logarithms and factoring integers on a quantum computer that take a number of steps which is polynomial in the input size, e.g., the number of digits of the integer to be factored. These two problems are generally considered hard on a classical computer and have been used as the basis of several proposed cryptosystems. (We thus give the first examples of quantum cryptanalysis.)

[1, 2]. Although he did not ask whether quantum mechanics conferred extra power to computation, he did show that a Turing machine could be simulated by the reversible unitary evolution of a quantum process, which is a necessary prerequisite for quantum computation. Deutsch [9, 10] was the first to give an explicit model of quantum computation. He defined both quantum Turing machines and quantum circuits and investigated some of their properties.

The next part of this paper discusses how quantum computation relates to classical complexity classes. We will thus first give a brief intuitive discussion of complexity classes for those readers who do not have this background. There are generally two resources which limit the ability of computers to solve large problems: time and space (i.e., memory). The field of analysis of algorithms considers the asymptotic demands that algorithms make for these resources as a function of the problem size. Theoretical computer scientists generally classify algorithms as efficient when the number of steps of the algorithms grows as a polynomial in the size of the input. The class of prob-



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- ▶ Can't run other quantum algorithms we care about.
- ▶ Hasn't managed to find any computation justifying its price.
- ▶ Hasn't managed to find any computation justifying 1% of its price.

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“We’re actually doing things that are making us think like, ‘hey this isn’t 50 years off, this is maybe just 10 years off, or 15 years off.’ It’s within reach.”
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- ▶ Also, Grover’s algorithm speeds up brute-force searches.
- ▶ Example: Only 2^{64} quantum operations to break AES-128;
 2^{128} quantum operations to break AES-256.



Physical cryptography: a return to the dark ages

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- ▶ Very limited functionality: e.g., no public-key signatures.

Is there any hope? Yes!

Post-quantum crypto is crypto that resists attacks by quantum computers.

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- ▶ PQCrypto 2014.
- ▶ New EU project, 2015–2018:
PQCRYPTO, Post-Quantum Cryptography for Long-term Security.





NSA announcements

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NSA comes late to the party and botches its grand entrance.

Post-quantum becoming mainstream

- ▶ PQCrypto 2016: 22–26 Feb in Fukuoka, Japan, with more than 200 participants



- ▶ NIST is calling for post-quantum proposals; expect a small competition.
- ▶ PQCrypto 2017 planned, will be in Utrecht, Netherlands.

Confidence-inspiring crypto takes time to build

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 - ▶ Integrate securely into real-world applications.
- ▶ Example: ECC introduced **1985**; big advantages over RSA. Robust ECC started to take over the Internet in **2015**.
- ▶ Post-quantum research can't wait for quantum computers!

ECC

ISS

80S

Even higher urgency for long-term confidentiality

- Today's encrypted communication is being stored by attackers and will be decrypted years later with quantum computers. Danger for human-rights workers, journalists, security research, lawyers, diplomats, health records . . .

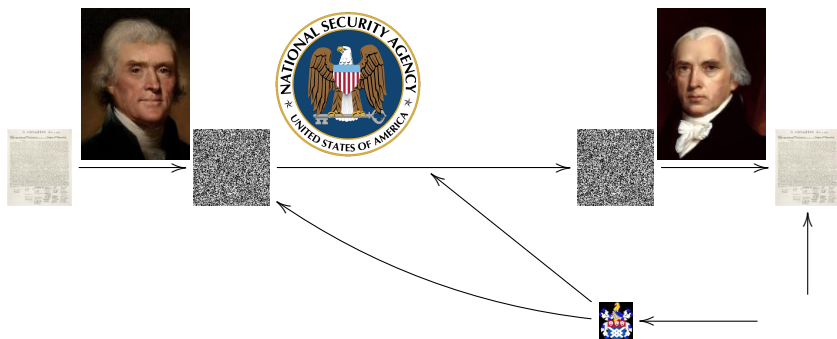


Post-quantum secret-key authenticated encryption



- ▶ Very easy solutions if secret key is long uniform random string:
 - ▶ “One-time pad” for encryption.
 - ▶ “Wegman–Carter MAC” for authentication.
- ▶ AES-256: Standardized method to expand 256-bit into string indistinguishable from long .
- ▶ AES introduced in 1998 by Daemen and Rijmen. Security analyzed in papers by dozens of cryptanalysts.
- ▶ No credible threat from quantum algorithms. Grover costs 2^{128} .

Post-quantum public-key encryption: code-based



- ▶ Jefferson uses Madison's public key  to encrypt.
- ▶ Madison uses his secret key  to decrypt.
- ▶ Code-based crypto proposed by McEliece in 1978 using Goppa codes.
- ▶ Almost as old as RSA, but much stronger security history.
- ▶ Many further improvements, e.g. Niederreiter system for smaller keys.

Security analysis

- ▶ Some papers studying algorithms for attackers:
1962 Prange; 1981 Omura; 1988 Lee–Brickell; 1988 Leon; 1989 Krouk;
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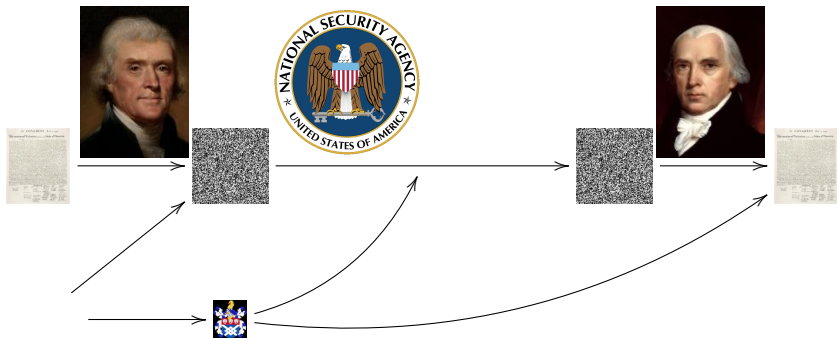
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- ▶ Post-quantum (Grover): below 2^{263} , above 2^{131} .

Post-quantum public-key signatures: hash-based



- ▶ Secret key , public key .
- ▶ Only one prerequisite: a good hash function, e.g. SHA3-512, ...
Hash functions map long strings to fixed-length strings.

Signature schemes use hash functions in handling

- ▶ Old idea: 1979 Lamport one-time signatures.
- ▶ 1979 Merkle extends to more signatures.

Pros and cons

Pros:

- ▶ Post quantum
- ▶ Only need secure hash function
- ▶ Small public key
- ▶ Security well understood
- ▶ Fast
- ▶ Proposed for standards: <https://tools.ietf.org/html/draft-irtf-cfrg-xmss-hash-based-signatures-01>

[\[Docs\]](#) [\[txt|pdf|xml|html\]](#) [\[Tracker\]](#) [\[WG\]](#) [\[Email\]](#) [\[Diff1\]](#) [\[Diff2\]](#) [\[Nits\]](#)

Versions: (draft-huelsing-cfrg-hash-sig-xmss)
00 01

Crypto Forum Research Group
Internet-Draft
Intended status: Informational
Expires: January 4, 2016

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TU Eindhoven
D. Butin
TU Darmstadt
S. Gazdag
genua GmbH
A. Mohaisen
Verisign Labs
July 3, 2015

XMSS: Extended Hash-Based Signatures draft-irtf-cfrg-xmss-hash-based-signatures-01

Abstract

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- ▶ Proposed for standards: <https://tools.ietf.org/html/draft-irtf-cfrg-xmss-hash-based-signatures-01>

Cons:

- ▶ Biggish signature
 - ▶ Stateful
- Adam Langley “for most environments it’s a huge foot-cannon.”

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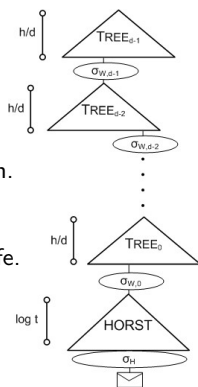
ELIMINATE



THE STATE

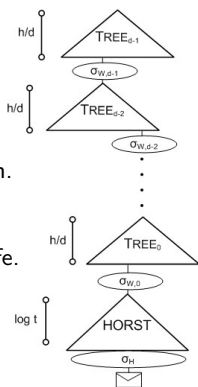
Stateless hash-based signatures

- ▶ Idea from 1987 Goldreich:
 - ▶ Signer builds huge tree of certificate authorities.
 - ▶ Signature includes certificate chain.
 - ▶ Each CA is a hash of master secret and tree position. This is deterministic, so don't need to store results.
 - ▶ **Random** bottom-level CA signs message. Many bottom-level CAs, so one-time signature is safe.



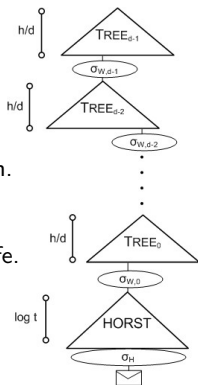
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- ▶ 0.041 MB: SPHINCS signature, new optimization of Goldreich. Modular, guaranteed as strong as its components (hash, PRNG). Well-known components chosen for 2^{128} post-quantum security.
sphincs.cr.yp.to



Many more post-quantum suggestions

- ▶ QC-MDPC: variant with much smaller keys, but is it secure?
- ▶ Many more code-based systems. Some broken, some not.
- ▶ NTRU: 1990s “lattice-based” system, similar to QC-MDPC. Security story less stable than code-based cryptography.
- ▶ Many more lattice-based systems. Some broken, some not. e.g., 2014 quantum break of 2009 Smart–Vercauteren system.
- ▶ Many multivariate-quadratic systems. Some broken, some not. Highlight: very small signatures.
- ▶ More exotic possibility that needs analysis: isogeny-based crypto. Highlight: supports DH.

Further resources

- ▶ General crypto/security links.
 - ▶ Talks: Security in Times of Surveillance 2014, 2015 and Post-Snowden Cryptography
 - ▶ Last week tonight: Encryption by John Oliver
 - ▶ Thomas Jefferson and Apple versus the FBI post by Bernstein
 - ▶ EFF and 46 Technology Experts Ask Court To Throw Out Unconstitutional Apple Order
- ▶ PQCrypto 2016 with slides and videos from lectures (incl. winter school)
- ▶ <https://pqcrypto.org>: Our survey site.
 - ▶ Many pointers: e.g., PQCrypto 2016.
 - ▶ Bibliography for 4 major PQC systems.
- ▶ <https://pqcrypto.eu.org>: PQCRYPTO EU project.
 - ▶ Expert recommendations.
 - ▶ Free software libraries. (Coming soon)
 - ▶ More benchmarking to compare cryptosystems. (Coming soon)
 - ▶ 2017: workshop and spring/summer school.
 - ▶ https://twitter.com/pqc_eu: PQCRYPTO Twitter feed.