

# The transition to post-quantum cryptography

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1 April 2022

# Cryptography



Sender  
"Alice"



Receiver  
"Bob"

Tsai Ing-wen picture credit: By 總統府, Attribution, [Wikimedia](#). Joe Biden picture credit: By Adam Schultz - White House, Public Domain, [Wikimedia](#).

# Cryptography



Sender  
"Alice"



Untrustworthy network  
"Eve"



Receiver  
"Bob"

- ▶ Motivation #1: Communication channels are spying on our data.
- ▶ Motivation #2: Communication channels are modifying our data.

Tsai Ing-wen picture credit: By 總統府, Attribution, [Wikimedia](#). Joe Biden picture credit: By Adam Schultz - White House, Public Domain, [Wikimedia](#).

# Cryptography



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- ▶ Motivation #1: Communication channels are spying on our data.
- ▶ Motivation #2: Communication channels are modifying our data.
- ▶ Literal meaning of cryptography: "secret writing".
- ▶ Achieves various security goals by secretly transforming messages.
  - ▶ Confidentiality: Eve cannot infer information about the content
  - ▶ Integrity: Eve cannot modify the message without this being noticed
  - ▶ Authenticity: Bob is convinced that the message originated from Alice

Tsai Ing-wen picture credit: By 總統府, Attribution, [Wikimedia](#). Joe Biden picture credit: By Adam Schultz - White House, Public Domain, [Wikimedia](#).

# Public-key vs. symmetric-key cryptography

## **Public-key cryptography**

Each user has 2 keys:  
a public key and a private key.

Public key can be posted online;  
private key must be kept secret.

Often can compute public key from private key.  
Other direction must be hard.

Can be used on Internet with unknown parties.  
Requires mathematically hard problem.

## **Symmetric-key cryptography**

Each pair of users shares a key.  
This key is symmetric between both users.

This key must be kept secret.

Symmetric systems often faster than  
public-key systems.  
Use latter to get symmetric key.

Requires that users have securely shared this key.  
Typically cheaper/faster than public-key crypto.

# Cryptographic tools

Many factors influence the security and privacy of data:

- ▶ Secure storage, physical security; access control.
- ▶ Protection against alteration of data  
⇒ public-key signatures, message-authentication codes.
- ▶ Protection of sensitive content against reading  
⇒ encryption (public-key or symmetric-key).

Many more security goals studied in cryptography

- ▶ Protecting against denial of service.
- ▶ Stopping traffic analysis.
- ▶ Securely tallying votes.
- ▶ Searching in and computing on encrypted data.
- ▶ ...

# Cryptanalysis

- ▶ Cryptanalysis is the study of security of cryptosystems.
- ▶ Breaking a system can mean that the hardness assumption was not hard or that it just was not as hard as previously assumed.
- ▶ Public cryptanalysis is ultimately constructive – ensure that secure systems get used, not insecure ones.
- ▶ Weakened crypto ultimately backfires – attacks today because of crypto wars in the 90s.
- ▶ Good arsenal of general approaches to cryptanalysis. There are some automated tools.
- ▶ This area is constantly under development; researchers revisit systems continuously.



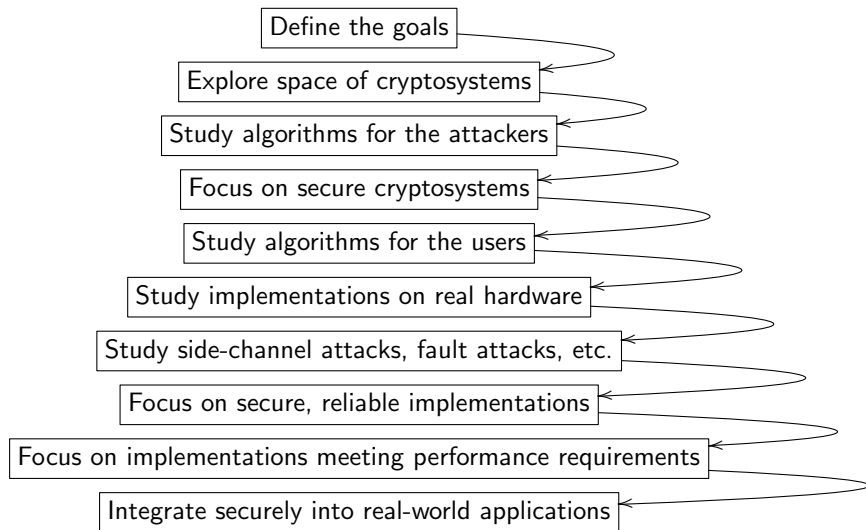




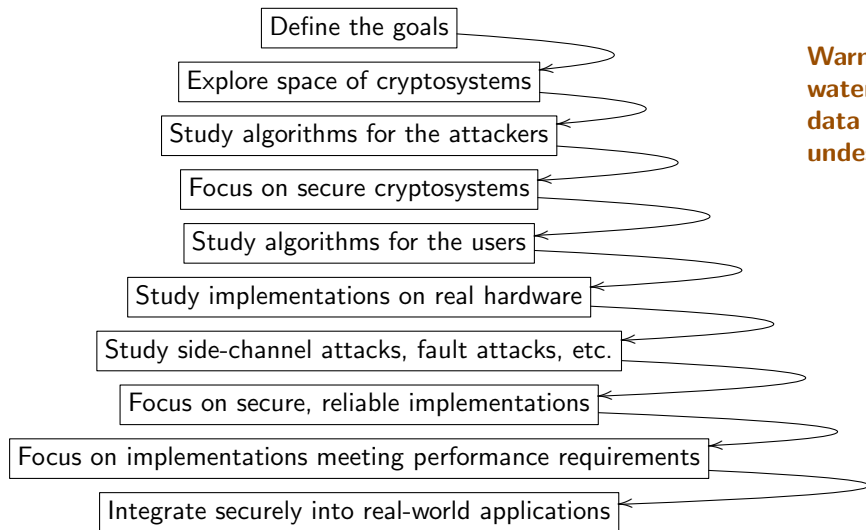
# Security assumptions

- ▶ Hardness assumptions at the basis of all public-key and essentially all symmetric-key systems result from (failed) attempts at breaking systems.
- ▶ Security “proofs” are built only on top of those assumptions.  
These relate the hardness of breaking a bigger system to the hardness of these assumptions.
- ▶ A solid symmetric system is required to be as strong as exhaustive key search.
- ▶ For public-key systems the best attacks are faster than exhaustive key search.  
Parameters are chosen to ensure that the best attack is infeasible.

# Many stages of cryptographic research from design to deployment



# Many stages of cryptographic research from design to deployment



**Warning:**  
waterfall  
data flow,  
undesirable.

## Key size recommendations

|                           | Parameter                  | Legacy | Future System Use |           |
|---------------------------|----------------------------|--------|-------------------|-----------|
|                           |                            |        | Near Term         | Long Term |
| Symmetric Key Size        | $k$                        | 80     | 128               | 256       |
| Hash Function Output Size | $m$                        | 160    | 256               | 512       |
| MAC Output Size*          | $m$                        | 80     | 128               | 256       |
| RSA Problem               | $\ell(n) \geq$             | 1024   | 3072              | 15360     |
| Finite Field DLP          | $\ell(p^n) \geq$           | 1024   | 3072              | 15360     |
|                           | $\ell(p), \ell(q) \geq$    | 160    | 256               | 512       |
| ECDLP                     | $\ell(q) \geq$             | 160    | 256               | 512       |
| Pairing                   | $\ell(p^{k \cdot n}) \geq$ | 1024   | 6144              | 15360     |
|                           | $\ell(p), \ell(q) \geq$    | 160    | 256               | 512       |

- ▶ Source: ECRYPT-CSA “Algorithms, Key Size and Protocols Report” (2018).
- ▶ These recommendations take into account attacks known today.
- ▶ Use extrapolations to larger problem sizes.
- ▶ Attacker power typically limited to  $2^{128}$  operations (less for legacy).
- ▶ More to come on long-term security ...

## Summary: current state of the art

- ▶ Currently used crypto (check the lock icon in your browser) starts with RSA, Diffie-Hellman (DH) in finite fields, or elliptic-curve Diffie-Hellman (ECDH).
- ▶ Older standards are RSA or elliptic curves from NIST (or Brainpool), e.g. NIST P256 or ECDSA.
- ▶ Internet currently moving over to [Curve25519](#) (Bernstein) and [Ed25519](#) (Bernstein, Duif, Lange, Schwabe, and Yang).
- ▶ For symmetric crypto, TLS (the protocol behind https) uses AES or ChaCha20 and some MAC, e.g. AES-GCM or ChaCha20-Poly1305. High-end devices have support for AES-GCM, smaller ones do better with ChaCha20-Poly1305.
- ▶ Security is getting better. Some obstacles: bugs; untrustworthy hardware.



# Algorithms for Quantum Computation: Discrete Logarithms and Factoring

Peter W. Shor  
AT&T Bell Labs  
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600 Mountain Ave.  
Murray Hill, NJ 07974, USA

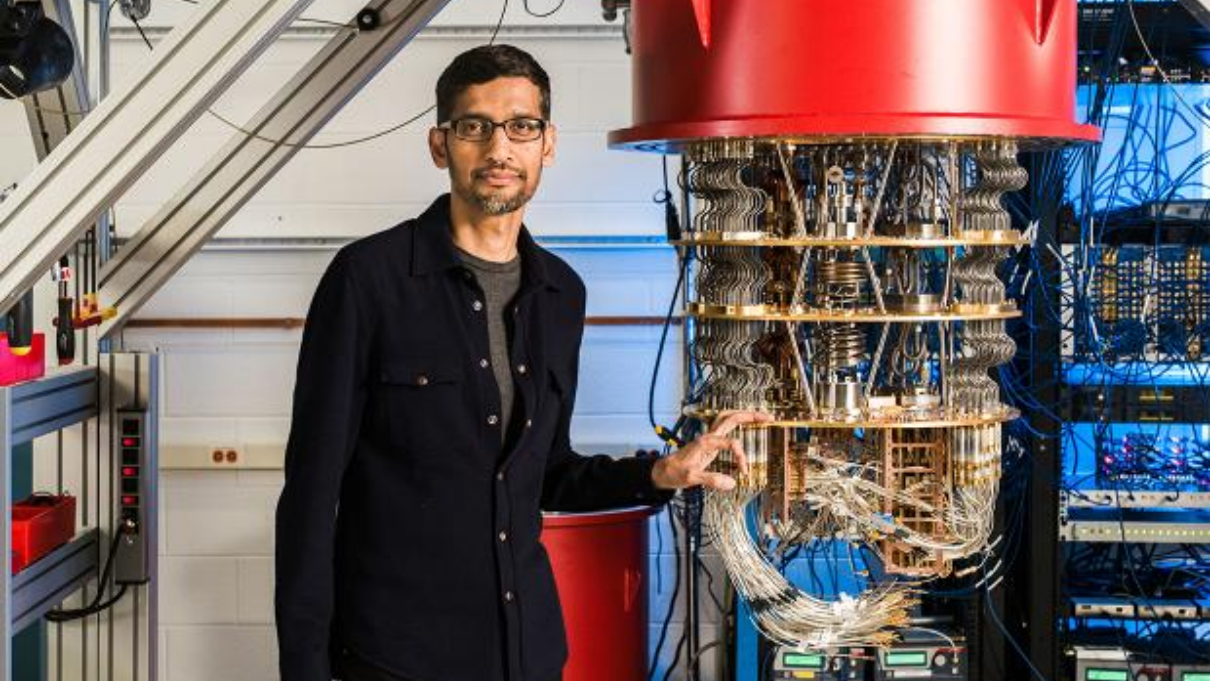
## Abstract

*A computer is generally considered to be a universal computational device; i.e., it is believed able to simulate any physical computational device with a cost in computation time of at most a polynomial factor. It is not clear whether this is still true when quantum mechanics is taken into consideration. Several researchers, starting with David Deutsch, have developed models for quantum mechanical computers and have investigated their compu-*

[1, 2]. Although he did not ask whether quantum mechanics conferred extra power to computation, he did show that a Turing machine could be simulated by the reversible unitary evolution of a quantum process, which is a necessary prerequisite for quantum computation. Deutsch [9, 10] was the first to give an explicit model of quantum computation. He defined both quantum Turing machines and quantum circuits and investigated some of their properties.

The next part of this paper discusses how quantum computation relates to classical complexity classes. We will

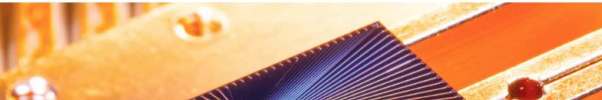




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# Quantum computing could end encryption within five years, says Google boss



Mr Pichai said a combination of artificial intelligence and quantum would "help us tackle some of the biggest problems we see", but said it was important encryption evolved to match this.

"In a five to ten year time frame, quantum computing will break encryption as we know it today."

This is because current encryption methods, by which information such as texts or passwords is turned into code to make it unreadable, rely upon the fact that classic computers would take billions of years to decipher that code.

Quantum computers, with their ability to be

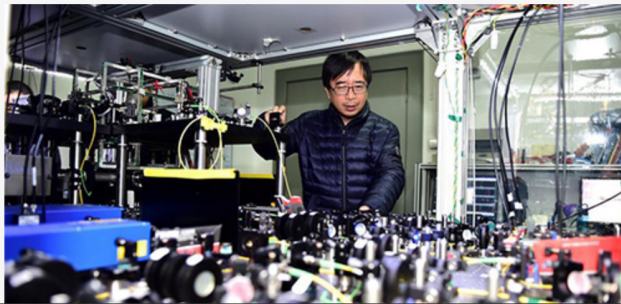
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PHOTOS

## Chinese researchers expect quantum leap in computing, challenging Google's supremacy

Source: Global Times Published: 2020/8/26 14:58:42

     19



SOURCE / ECONOMY

# Chinese researchers achieve quantum advantage in two mainstream routes

By Global Times

Published: Oct 26, 2021 01:18 PM





# National Academy of Sciences (US)

4 December 2018: [Report on quantum computing](#)

**Don't panic.** “Key Finding 1: Given the current state of quantum computing and recent rates of progress, it is highly unexpected that a quantum computer that can compromise RSA 2048 or comparable discrete logarithm-based public key cryptosystems will be built within the next decade.”

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**Panic.** “Key Finding 10: Even if a quantum computer that can decrypt current cryptographic ciphers is more than a decade off, the hazard of such a machine is high enough—and the time frame for transitioning to a new security protocol is sufficiently long and uncertain—that prioritization of the development, standardization, and deployment of post-quantum cryptography is critical for minimizing the chance of a potential security and privacy disaster.”

“[Section 4.4:] In particular, all encrypted data that is recorded today and stored for future use, will be cracked once a large-scale quantum computer is developed.”

# Commonly used systems



Sender  
"Alice"



Untrustworthy network  
"Eve"



Receiver  
"Bob"

Cryptography with symmetric keys

**AES-128. AES-192. AES-256. AES-GCM. ChaCha20. HMAC-SHA-256. Poly1305. SHA-2. SHA-3. Salsa20.**

Cryptography with public keys

**BN-254. Curve25519. DH. DSA. ECDH. ECDSA. EdDSA. NIST P-256. NIST P-384. NIST P-521. RSA encrypt. RSA sign. secp256k1.**



# Commonly used systems



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Untrustworthy network  
"Eve" with quantum computer



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**BN-254. Curve25519. DH. DSA. ECDH. ECDSA. EdDSA. NIST P-256. NIST P-384. NIST P-521. RSA encrypt. RSA sign. secp256k1.**

# Symmetric-key authenticated encryption



Sender  
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Untrustworthy network  
"Eve" with quantum computer



Receiver  
"Bob"

- ▶ Very easy solutions **if Alice and Bob already share long secret key  $k$** :
  - ▶ "One-time pad" for confidentiality.
  - ▶ "Wegman–Carter MAC" for integrity and authenticity.
- ▶ AES-256: Standardized method to expand **short secret key** (256-bit  $k$ ) into string indistinguishable from long secret key.
- ▶ AES introduced in 1998 by Daemen and Rijmen. Security analyzed in papers by dozens of cryptanalysts.
- ▶ No credible threat from quantum algorithms. Grover costs  $2^{128}$ .
- ▶ Some results assume attacker has quantum access to computation, then some systems are weaker ... but I'd know if my laptop had turned into a quantum computer.

# Post-quantum cryptography

Cryptography under the assumption that the attacker has a quantum computer.

- ▶ 1994: Shor's quantum algorithm. 1996: Grover's quantum algorithm.  
Many subsequent papers on quantum algorithms: see [quantumalgorithmzoo.org](https://quantumalgorithmzoo.org).
- ▶ 2003: Daniel J. Bernstein introduces term [Post-quantum cryptography](#).
- ▶ 2006: First International Workshop on Post-Quantum Cryptography. PQCrypto 2006, 2008, 2010, 2011, 2013, 2014, 2016, 2017, 2018, 2019, 2020, 2021, (soon) 2022.
- ▶ 2015: NIST hosts its first workshop on post-quantum cryptography.
- ▶ 2016: NIST announces a standardization project for post-quantum systems.
- ▶ 2017: Deadline for submissions to the NIST competition.
- ▶ 2019: Second round of NIST competition begins.
- ▶ 2020: Third round of NIST competition begins.
- ▶ 2021 2022 ~~“not later than the end of March”~~: NIST announces first selections.
- ▶ 2023/2024?: NIST issues post-quantum standards.

## PQCRYPTO initial recommendations of long-term secure post-quantum systems (2015)

Daniel Augot, Lejla Batina, Daniel J. Bernstein, Joppe Bos,  
Johannes Buchmann, Wouter Castryck, Orr Dunkelman,  
Tim Güneysu, Shay Gueron, Andreas Hülsing,  
Tanja Lange, Mohamed Saied Emam Mohamed,  
Christian Rechberger, Peter Schwabe, Nicolas Sendrier,  
Frederik Vercauteren, Bo-Yin Yang

# Initial recommendations (PQCRYPTO, 2015)

- ▶ **Symmetric encryption** Thoroughly analyzed, 256-bit keys:
  - ▶ AES-256
  - ▶ Salsa20 with a 256-bit key

Evaluating: Serpent-256, ...

- ▶ **Symmetric authentication** Information-theoretic MACs:
  - ▶ GCM using a 96-bit nonce and a 128-bit authenticator
  - ▶ Poly1305
- ▶ **Public-key encryption** McEliece with binary Goppa codes:
  - ▶ length  $n = 6960$ , dimension  $k = 5413$ ,  $t = 119$  errors

Evaluating: QC-MDPC, Stehlé-Steinfeld NTRU, ...

- ▶ **Public-key signatures** Hash-based (minimal assumptions):
  - ▶ XMSS with any of the parameters specified in CFRG draft
  - ▶ SPHINCS-256

Evaluating: HFEv-, ...

# Major categories of public-key post-quantum systems

- ▶ **Code-based** encryption: McEliece cryptosystem has survived since 1978. Short ciphertexts and large public keys. Security relies on hardness of decoding error-correcting codes.
- ▶ **Hash-based** signatures: very solid security and small public keys. Require only a secure hash function (hard to find second preimages).
- ▶ **Isogeny-based** encryption: new kid on the block, promising short keys and ciphertexts and non-interactive key exchange. Security relies on hardness of finding isogenies between elliptic curves over finite fields.
- ▶ **Lattice-based** encryption and signatures: possibility for balanced sizes. Security relies on hardness of finding short vectors in some (typically special) lattice.
- ▶ **Multivariate-quadratic** signatures: short signatures and large public keys. Security relies on hardness of solving systems of multivariate equations over finite fields.

Warning: These are categories of mathematical problems;  
individual systems may be totally insecure if the problem is not used correctly.

We have a good understanding of what a quantum computer can do,  
but new systems need more analysis.

## More details of what NIST has said

[2020.07.22](#) NIST: “NIST intends to select a small number of the finalists for standardization at the end of the third round. In addition, NIST expects to standardize a small number of the alternate candidates (most likely at a later date). . . . If NIST’s confidence in better performing signature algorithms is shaken by new analysis , SPHINCS+ could provide an immediately available algorithm for standardization at the end of the third round.”

[2021.12.07](#) NIST: “NIST will be selecting the first post-quantum standards for KEMs (and digital signatures) around the end of December or sometime in early January.”

[2022.02.08](#) Nature article “The race to save the Internet from quantum hackers”: “In the next few months, the institute will select two algorithms for each application. It will then begin to draft standards for one, while keeping the other as a reserve in case the first choice ends up being broken by an unexpected attack, quantum or otherwise.”

[2022.02.09](#) NIST: “We hope to be able to announce the results and report not later than the end of March.”

[2022.03.31](#) NIST: “We ask for a little bit more patience since we are not ready to make the announcement today. We still expect to make it very soon.”

# The lattice decisions: not easy to predict

2020.07.22 NIST: “As CRYSTALS-KYBER, NTRU, and SABER are all structured lattice schemes, NIST intends to select, at most, one of these finalists to be standardized. The same is true for the finalist signature schemes CRYSTALS-DILITHIUM and FALCON. In NIST’s current view, these structured lattice schemes appear to be the most promising general-purpose algorithms for public-key encryption/KEM and digital signature schemes.”

Hard for community to figure out what NIST is going to do:

- ▶ Kyber faster than SABER on big CPUs. SABER faster in hardware.  
Kyber more fashionable.
- ▶ NTRU: avoids several patent questions, but slower keygen and less fashionable.
- ▶ Falcon: much smaller sigs than Dilithium, but harder to implement and less fashionable.
- ▶ There are some claims regarding impact of performance on applications.  
Not clear what weight NIST will put on these claims.



# How does PQC affect protocols?

- Length fields don't fit.

A photograph of an elephant sitting in the driver's seat of a light blue vintage car, looking out the windshield. The car is parked on a dark surface.

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- Embedded Use Cases in Industry
- Transition from Pre- to Post-Quantum Cryptography
- Dedicated PQC Schemes for Embedded Devices
- Secure Embedded Implementations of PQC

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Please do not forget to bring your own laptop and a good internet connection.

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  - ⇒ Restrict to systems that fit, if any,
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Photo by: Roy Mookerjee (2019), The Elephant in the Driver's Seat, CC BY-SA

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- ▶ Speed, resources.  
Combined schemes take about twice the time.

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- ▶ Interface mismatch – KEM instead of key exchange,  
stateful hash-based signatures fit some applications.

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- ▶ Validation and certification schemes are not yet updated.
  - ⇒ Combine pre-and post-quantum schemes, certification only applies to pre-quantum scheme.
  - For such *hybrid* schemes, ensure that as strong as strongest not as weak as weakest.

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- ▶ Validation and certification schemes are not yet updated.
  - ⇒ Combine pre-and post-quantum schemes, certification only applies to pre-quantum scheme.
  - For such *hybrid* schemes, ensure that as strong as strongest not as weak as weakest.
- ▶ New security assumptions, new proofs, lots of new code.



The poster for the Lorentz center workshop features a photograph of an elephant sitting in the driver's seat of a light blue vintage car. The text on the poster includes the title 'Post-Quantum Cryptography for Embedded Systems', the dates '5 - 9 October 2020, Leiden, the Netherlands', and the location 'Online Workshop'. It lists scientific organizers: Andreas Hülsing (Eindhoven University of Technology), Tanja Lange (Eindhoven University of Technology), Ruben Niederhagen (Fraunhofer SIT), Simona Samardjiska (Radboud University), and Marc Stöttinger (Continental AG). The topics listed are: Embedded Use Cases in Industry, Transition from Pre- to Post-Quantum Cryptography, Dedicated PQC Schemes for Embedded Devices, and Secure Embedded Implementations of PQC. At the bottom, it mentions 'The Lorentz Center organizes international workshops for researchers in all scientific disciplines to aim to foster an international dialogue on collaborative research, discussions and networking. Registration and more information: <https://www.lorentzcenter.nl>'.

Lorentz center  
Post-Quantum Cryptography  
for Embedded Systems  
Online Workshop  
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Scientific Organizers

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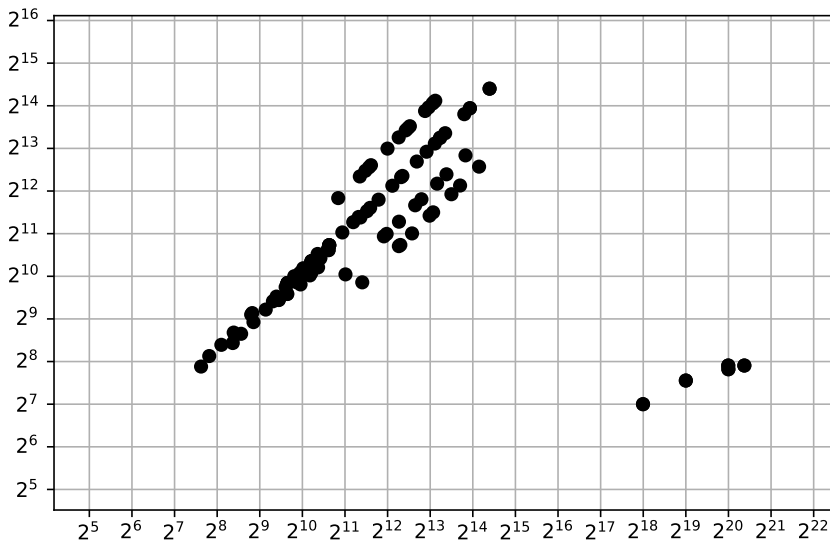
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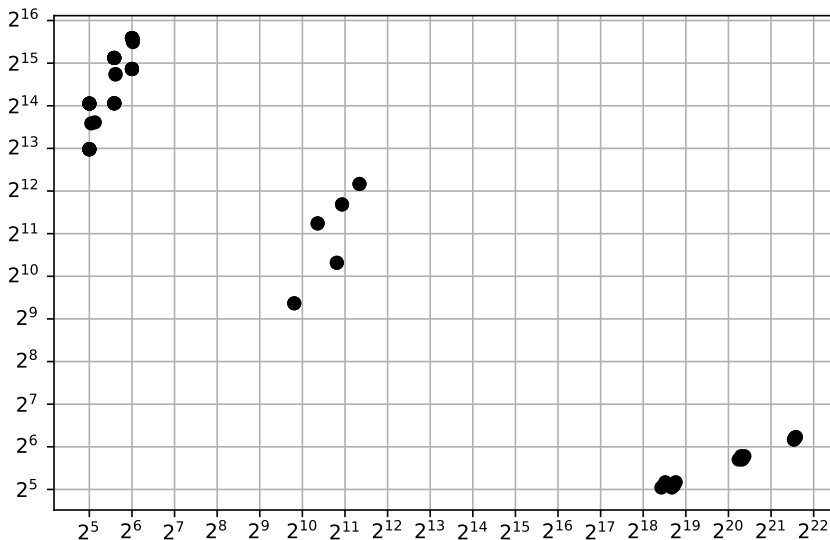
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[www.lorentzcenter.nl](https://www.lorentzcenter.nl)

## Encryption (KEM): ciphertext size (vertical) vs. public-key size (horizontal)



## Signatures: signature size (vertical) vs. public-key size (horizontal)



# Deployment issues & solutions

- ▶ Different recommendations for rollout in different risk scenarios:
  - ▶ Use most efficient systems with ECC or RSA, to ease usage and gain familiarity.
  - ▶ Use most conservative systems (possibly with ECC), to ensure that data really remains secure.
- ▶ Protocol integration and implementation problems:
  - ▶ Key sizes or message sizes are larger for post-quantum systems, but IPv6 guarantees only delivery of  $\leq 1280$ -byte packets, TLS software has length limits, etc.
  - ▶ Google [experimented](#) with larger keys and noticed delays and dropped connections.
  - ▶ Long-term keys require extra care (reaction attacks).
- ▶ Some libraries exist, quality is getting better.
- ▶ [Google](#) and [Cloudflare](#) are running some experiments of including post-quantum systems into TLS.

# Timeline of widely used software adding post-quantum options

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These encryption layers are *added* to X25519 encryption (ECC).

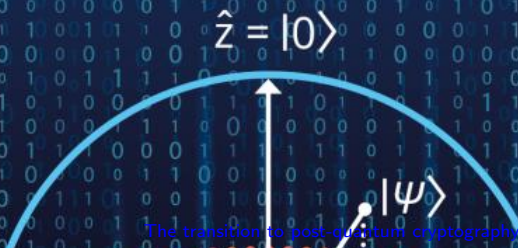
If lattices are completely broken, still have pre-quantum security.

# Post-Quantum Cryptography: Current state and quantum mitigation



Ward Beullens, Jan-Pieter D'Anvers, Andreas Hülsing,  
Tanja Lange, Lorenz Panny, Cyprien de Saint Guilhem, Nigel P. Smart.  
Evangelos Rekleitis, Angeliki Aktypi, Athanasios-Vasileios Grammatopoulos.

EUROPEAN UNION AGENCY  
FOR CYBERSECURITY



# ENISA report: Current state and quantum mitigation

## Chapters

1. Introduction
2. Families of Post-Quantum Algorithms
3. Security Notions and Generic Transforms
4. NIST Round 3 Finalists
5. Alternate Candidates
6. Quantum Mitigation
  - 6.1 Hybrid schemes
  - 6.2 Protective measures for pre-quantum cryptography

Report available from [ENISA's website](#).

# Hybrid schemes – implementation choices

Combine one (or more) pre-quantum schemes with one (or more) post-quantum schemes.

## **Signatures:**

All individual signatures must be valid for the hybrid signature to be valid.



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## **Signatures:**

All individual signatures must be valid for the hybrid signature to be valid.

## **DH / KEM:**

Use KDF (key-derivation function) on concatenation of keys or consume iteratively.

Different options to hybridize

- ▶ Execute pre- and post-quantum next to each other.
- ▶ Wrap PQC inside pre-quantum (benefit for length fields).
- ▶ Wrap pre-quantum inside PQC (limit the attack surface – quantum attacker cannot even break pre-quantum scheme).

# US ANSI X9 on post-quantum hybrids

2021: “As we transition from classical cryptography to post-quantum cryptography (PQC), there is a need to understand the proper ways to use both methods simultaneously. PQC methods will not be able to be used as a direct replacement in all cases. And the confidence and broad acceptance of PQC methods will not be as great as classical cryptography.

**Simultaneous use of both classical cryptography and PQC methods for both security and acceptance** is required during a transition and may be required long term as well. There are improper and insecure ways of implementing a hybrid of classical and PQC methods. Specifying the proper methods of using both are required.” (emphasis added)

## French ANSSI on post-quantum hybrids

2022: “Although this new post-quantum toolbox may seem handy for developers, the maturity level of the post-quantum algorithms presented to the NIST process should not be overestimated. Many aspects lack cryptanalytical hindsight or are still research topics, e.g. analysis of the difficulty of the underlying problem in the classical and quantum computation models, dimensioning, integration of schemes in protocols and more importantly the design of secure implementations. This situation will probably last some time after the publication of NIST standards. **Acknowledging the immaturity of PQC is important: ANSSI will not endorse any direct drop-in replacement of currently used algorithms in the short/medium term.** However, this immaturity should not serve as an argument for postponing the first deployments.” (emphasis added)

# US National Security Agency and Department of Homeland Security

**2021 NSA:** “NSA is waiting for the NIST process to be completed and for standards to be published. . . . NSS customers are reminded that NSA does not recommend and policy does not allow implementing or using unapproved, non-standard or experimental cryptographic algorithms. The field of quantum-resistant cryptography is no exception.”

**2021 DHS:** **Do not use** “post-quantum cryptographic industry products until standardization, implementation, and testing of replacement products with approved algorithms are completed by NIST.”

**2022 NSA:** “NSA does not expect to approve post-quantum algorithms with any kind of ‘but just to be safe, combine with an older algorithm’ guidance”—in other words, to sell post-quantum products to U.S. government, companies have to turn off ECC.

# Protective measures for pre-quantum cryptography

Aka poor-man's PQC

**Premise:** Known/slowly changing set of peers.

This fits email, messaging (Signal, etc.), most enterprise setups.

Does not fit web servers.

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**Option 2:** Have updatable secret per peer, include this in KDF.

Update per-peer secret with each new public-key operation.

Initial secret exchanged out of band, or exchange is not observed.

More complicated dataflow, e.g., do not overwrite without confirmation that peer can update, but full forward secrecy.

Details worked out in [RFC 6189](#) on ZRTP, see also section 6.2 of the [ENISA report](#).



# PQConnect: An Automated Boring Protocol for Quantum-Secure Tunnels

Daniel J. Bernstein, Tung Chou, Kai-Min Chung, Tanja Lange, Jonathan Levin, Lorenz Panny,  
Jon A. Solworth, Bo-Yin Yang.

# Different deployment strategy

- ▶ Do not patch PQC onto existing network protocols, but add a new layer with superior security.

# Different deployment strategy

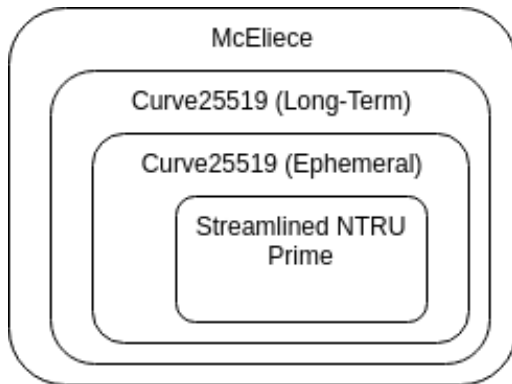
- ▶ Do not patch PQC onto existing network protocols, but add a new layer with superior security.
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- ▶ Add support for VPN-like tunnels to clients and servers.

## Different deployment strategy

- ▶ Do not patch PQC onto existing network protocols, but add a new layer with superior security.
- ▶ Can be gradually deployed.
- ▶ Add support for VPN-like tunnels to clients and servers.
- ▶ PQConnect is designed for security, handshake and ratcheting proven using Tamarin prover (formal verification tool).
- ▶ Use Curve25519 (pre-quantum) and Classic McEliece (conservative PQC) for long-term identity keys.
- ▶ Use Curve25519 (pre-quantum) and Streamlined NTRU Prime (PQC) for ephemeral keys.

## PQConnect handshake: Nesting schemes

Most conservative system on the outside.



Attacker can see long-term Curve25519 identity key,  
can break it with a quantum computer,  
but cannot obtain DH value as client's share is wrapped.

# Key ratchet advances by message and time

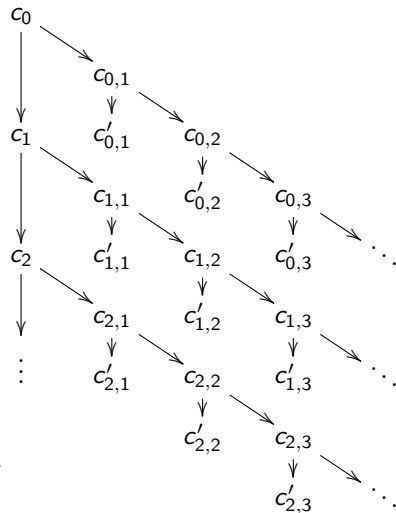
Complete protocol follows picture on previous slide.  
All systems linked together to generate initial key  $c_0$ .  
Keys are updated (ratcheted) to protect against later decryption by theft of computer equipment.  
Immediately advance ratchet in 3 ways:

- ▶ New epoch master key:  $c_1$ .
- ▶ New branch keys:  $c_{0,1}, c_{0,2}$ .
- ▶ New message key:  $c'_{0,1}$ .

Delete key as soon as no longer needed.  
Message keys can deal with delayed transmissions.

More information on protocol:

<https://research.tue.nl/en/studentTheses/pqconnect>



## Further information

- ▶ <https://pqcrypto.org> our overview page.
- ▶ PQCrypto 2016, PQCrypto 2017, PQCrypto 2018, PQCrypto 2019, PQCrypto 2020, PQCrypto 2021 with many slides and videos online.
- ▶ <https://pqcrypto.eu.org>: PQCRIPTO EU Project.
  - ▶ PQCRIPTO [recommendations](#).
  - ▶ Free software libraries ([libpqcrypto](#), [pqm4](#), [pqhw](#)).
  - ▶ Many reports, scientific articles, (overview) talks.
- ▶ YouTube channel [Tanja Lange: Post-quantum cryptography](#).
- ▶ <https://2017.pqcrypto.org/school>: PQCRIPTO summer school with 21 lectures on video, slides, and exercises.
- ▶ <https://2017.pqcrypto.org/exec> and <https://pqcschool.org/index.html>: Executive school (less math, more perspective).
- ▶ [Quantum Threat Timeline](#) from Global Risk Institute, 2019; [2021 update](#).
- ▶ [Status of quantum computer development](#) (by German BSI).
- ▶ [NIST PQC competition](#).